

- Faculté des sciences économiques
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## Inferential statistics and test theory (5ST2004)

Filières concernées	Nombre d'heures	Validation	Crédits ECTS
<b>Master en méthodologie d'enquête et d'opinion publique (avant 2015)</b>	<b>Cours: 4 ph</b>	<b>écrit: 2 h</b>	6
<b>Master en statistique (avant 2015)</b>	<b>Cours: 4 ph</b>	<b>écrit: 2 h</b>	6

ph=période hebdomadaire, pg=période globale, j=jour, dj=demi-jour, h=heure, min=minute

### Période d'enseignement:

- Semestre Automne

### Equipe enseignante:

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### Objectifs:

Introducing the theoretical background of Mathematical Statistics. Learning how to build, judge the performance, improve and compare the statistical procedures of point estimation, interval estimation and hypotheses testing.

### Contenu:

1. Statistical model
  - a. Definition, parametric and nonparametric models
  - b. Sampling models
  - c. Exponential families
  - d. Location-scale families
2. Point estimation
  - a. Statistics and estimators
  - b. Classical methods of obtaining estimators: empirical estimation, method of moments, maximum likelihood method
  - c. Criteria to judge the performance of estimators: consistency, bias, risk, Fisher information, Cramer-Rao inequality
  - d. Improving estimators: sufficient statistic, Rao-Blackwell and Lehmann-Scheffé theorems
  - e. Asymptotic behaviour: Asymptotic normality,  $\Delta$ -method, the particular cases of the empirical estimators, the maximum likelihood estimators and method of moments estimators
3. Interval estimation
  - a. Exact confidence intervals
  - b. Asymptotic confidence intervals
4. Testing statistical hypothesis
  - a. Introduction and definition : hypothesis, test statistics and critical regions, type I and type II errors, level of significance, power, p-value, bias, UMP tests, asymptotic tests
  - b. Parametric tests: Neyman-Pearson Lemma, nonrandomized and randomized tests
  - c. The particular case of gaussian samples: Hypothesis about the mean, hypothesis about the variance
  - d. Nonparametric tests: Kolmogorov test,  $\chi^2$  tests, Kolmogorov-Smirnov test, Mann-Whitney test

### Forme de l'évaluation:

E : 2-hour final written test during the end-of-semester examination session.

Reexamination session (August-September) : 2h written test

### Documentation:

- J. Shao, *Mathematical Statistics*, 2nd edition, Springer, 2003  
R. Bartoszyński and M. Niewiadomska-Bugaj, *Probability and Statistical Inference*, Wiley series in Probability and Statistics, 1996.

### Pré-requis:

Probability Theory

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### **Inferential statistics and test theory (5ST2004)**

**Forme de l'enseignement:**

- 6 ECTS credits
- Compulsory course for master in statistics
- Autumn Semester
- Course : 2 hours / Exercises : 2 hours