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### Inferential statistics and test theory (3ST2002)

Filières concernées	Nombre d'heures	Validation	Crédits ECTS
<b>Master en statistique</b>	<b>Cours: 4 ph</b>	<a href="#">Voir ci-dessous</a>	6

ph=période hebdomadaire, pg=période globale, j=jour, dj=demi-jour, h=heure, min=minute

#### Période d'enseignement:

- Semestre Automne

#### Equipe enseignante

Professeur : Jean-Yves Dauxois  
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#### Contenu

1. Statistical model
  - a. Definition, parametric and nonparametric models
  - b. Sampling models
  - c. Exponential families
  - d. Location-scale families
2. Point estimation
  - a. Statistics and estimators
  - b. Classical methods of obtaining estimators: empirical estimation, method of moments, maximum likelihood method
  - c. Criteria to judge the performance of estimators: consistancy, bias, risk, Fisher information, Cramer-Rao inequality
  - d. Improving estimators: sufficient statistic, Rao-Blackwell and Lehmann-Scheffé theo-rems
  - e. Asymptotic behaviour: Asymptotic normality,  $\sqrt{n}$ -method, the particular cases of the empirical estimators, the maximum likelihood estimators and method of moments estimators
3. Interval estimation
  - a. Exact confidence intervals
  - b. Asymptotic confidence intervals
4. Testing statistical hypothesis
  - a. Introduction and definition : hypothesis, test statistics and critical regions, type I and type II errors, level of significance, power, p-value, bias, UMP tests, asymptotics tests
  - b. Parametric tests: Neyman-Pearson Lemma, nonrandomized and randomized tests
  - c. The particular case of gaussian samples: Hypothesis about the mean, hypothesis about the variance
  - d. Nonparametric tests: Kolmogorov test, Chi2 tests, Kolmogorov-Smirnov test, Mann-Whitney test

#### Forme de l'évaluation

2 hours written exam at any exams session.

#### Documentation

J. Shao, Mathematical Statistics, 2nde edition, Springer, 2003  
 R. Bartoszynski and M. Niewiadomska-Bugaj, Probability and Statistical Inference, Wiley series in Probability and Statistics, 1996.

#### Pré-requis

Probability Theory

#### Forme de l'enseignement

- 6 ECTS credits
- Compulsory course for master in statistics
- Autumn Semester
- Course : 2 hours / Exercises : 2 hours